

# CHAOS2024 - Hybrid

## 17<sup>th</sup>Chaotic Modeling and Simulation International Conference 11 - 14 June, 2024, Chania, Crete, Greece

http://www.cmsim.org/chaoschania2024.html

Book of Abstracts.

**Special Session on Localized Excitations in Nonlinear Lattices** Organizers: Jānis Bajārs and Juan FR Archilla



### Talks (alphabetical order):

•	Juan F.R. Archilla, Jānis Bajārs, Yusuke Doi, Masayuki Kimura. Nonlin	ıear
	Energy and Charge Transport in Silicates. Experiments and semiclass	ical
	models	3

- <u>Pavel Selyshchev</u>. *Development of nonmonotonically propagating annealing of defects with oscillating temperature at the wave front .......*9

## Nonlinear Energy and Charge Transport in Silicates. Experiments and semiclassical models.

Juan F.R. Archilla<sup>1,\*</sup>, Jānis Bajārs<sup>2</sup>, Yusuke Doi<sup>3</sup>, Masayuki Kimura<sup>4</sup>

<sup>1</sup>Universidad de Sevilla, Sevilla, Spain, <sup>2</sup>University of Latvia, Riga, Latvia <sup>3</sup>Osaka University, Osaka, Japan, <sup>4</sup>Setsunan University, Osaka, Japan E-mail<sup>\*</sup>: archilla@us.es

**Abstract:** Experiments with silicates bombarded by alpha particles show the transport of charge and energy without the need of an electric field, the energy and momentum provided by the alpha particles. We construct two semiclassical models to model the observed phenomena, a phenomenological one, used as a test model to develop and refine the theory, and other obtained from physical principles and empiric potentials. For the latter the propagation of charge is difficult to achieve, but there are exact neutral excitations, transporting energy. We also present provisional results on the thermalized lattice.

Keywords: Nonlinear excitations. Charge transport. Energy transport. Semiclassical lattices. Silicates.

#### References

[1] JFR Archilla; J Bajārs, Y Doi, M Kimura. A semiclassical model for charge transfer along ion chains in silicates. J. Phys: Conf. Ser. (to appear), arXiv:2308.1518 (2024)

[2] Spectral Properties of Exact Polarobreathers in Semiclassical Systems. JFR Archilla; J Bajārs.

Axioms 12, 5 (2023) 437/1-26.

[3] FM Russell; JFR Archilla; JL Mas. Quodon current in tungsten and consequences for tokamak fusion reactors. Phys. Status Solidi RRL 18 (2023) 2300297/1-5.

[4] JFR Archilla, Y Doi, M Kimura. Pterobreathers in a model for a layered crystal with realistic potentials: Exact moving breathers in a moving frame. Phys. Rev E 100, 2 (2019) 022206/1-17.

Acknowledgments: The authors acknowledge the following projects and grants:

JFRA: MICINN PID2022-138321NB-C22, and travel grants from VII PPITUS-2024 of the University of Sevilla. JB: project from the Faculty of Physics, Mathematics and Optometry, University of Latvia (2024) YD: JSPS Kahenhi (C) No. 19K03654.

MK: JSPS Kakenhi (C) No. 21K03935

### Numerical integration of thermostated semiclassical Hamiltonian lattice equations

Jānis Bajārs<sup>1,\*</sup>, Juan F.R. Archilla<sup>2</sup>

<sup>1</sup>University of Latvia, Riga, Latvia; <sup>2</sup>Universidad de Sevilla, Sevilla, Spain E-mail<sup>\*</sup>: janis.bajars@lu.lv

**Abstract:** In this work, we develop computationally efficient splitting methods for semiclassical Hamiltonian lattice equations, where crystal lattice models are described by classical Hamiltonian dynamics, whereas an extra charge (electron or hole) is modeled as a quantum particle within the tight-binding approximation. Such models are of significant scientific importance. A particular application is hyperconductivity, i.e., the experimental observation of charge transport without the presence of an external electric field when a silicate is bombarded with alpha particles. The charge is carried by nonlinear lattice excitations. In the present work, the canonical equations for a semiclassical Hamiltonian describing the coupled lattice-charge dynamics are coupled to a gentle stochastic thermostat, which drives the system to the canonical distribution at a prescribed temperature with minimal perturbations to the Hamiltonian trajectories while at the same time ensuring the conservation of the charge probability. The properties of the proposed splitting methods are explored and numerically demonstrated on a phenomenological semiclassical Hamiltonian lattice model.

**Keywords:** semiclassical Hamiltonian dynamics; splitting methods; lattice models; stochastic thermostats; charge transfer; nonlinear localized excitations.

#### **References:**

[1] J.F.R. Archilla, J. Bajārs, Y. Doi and M. Kimura. A semiclassical model for charge transfer along ion chains in silicates. J. Phys: Conf. Ser. (to appear), arXiv:2308.1518 (2024).

[2] J.F.R. Archilla and J. Bajārs. *Spectral properties of exact polarobreathers in semiclassical systems*. Axioms 12, 5 (2023) 437/1-26.

[3] J. Bajārs and J.F.R. Archilla. Splitting methods for semi-classical Hamiltonian dynamics of charge transfer in nonlinear lattices. Mathematics 10, 19 (2022) 3460.

[4] F.M. Russell, M.W. Russell and J.F.R. Archilla. *Hyperconductivity in fluorphlogopite at 300 K and 1.1 T*. EPL 127,1 (2019) 16001.

Acknowledgments: The authors acknowledge the following projects and grants: J. Bajārs: project from the Faculty of Physics, Mathematics and Optometry, University of Latvia (2024); J.F.R. Archilla: MICINN PID2022-138321NB-C22, and travel grants from VII PPITUS-2024 of the Universidad de Sevilla.

### Soliton dynamics in an oscillating magnetic field

#### Larissa Brizhik

Bogolyubov Institute for Theoretical Physics, Kyiv, Ulraine E-mail<sup>\*</sup>: brizhik@bitp.kyiv.ua

**Abstract:** The talk is dedicated to 50 years of the Davydov's soliton [1]. The influence of oscillating magnetic field on the soliton dynamics is investigated [2]. It is shown that such dynamics is described by the system of coupled nonlinear equations, which in the continuum adiabatic approximation can be reduced to the modified nonlinear Schroedinger equation. Soliton dynamics is shown to depend essentially not only on the amplitude and frequency of the magnetic field, but also on its orientation. In the magnetic field parallel to the molecular chain axis soliton propagation is a composition of the "free" soliton coherent movement along the molecular chain and electron cyclotron oscillations in the perpendicular plain with the effective cyclotron frequency and mass, In the case of magnetic field perpendicular to molecular chain axis, soliton propagation along the chain is described by the modified nonlinear Schroedinger equation with the term in the right hand side, which is determined by the magnetic field. This equation is solved using the nonlinear perturbation theory [3]. It is shown that soliton parameters are functions oscillating in time with the frequency of the main harmonic, given by the frequency of the external field, and its higher multiple harmonics. Such complex soliton dynamics in the oscillating external magnetic field affects charge transport and, therefore, the processes, this transport is involved in, such as electroconductivity in low-dimensional systems used in micro- and nanoelectronics [4] or redox processes in living organisms [5].

**Keywords:** Davydov soliton, magnetic field, low-dimensional system, perturbation theory, mechanism of therapeutic effect of oscillating magnetic field

#### References

[1] A.S. Davydov, N.I. Kislukha, Solitary excitons in one-dimensional molecular chains. Phys. Status Solidi B 59, 465 (1973).

[2] L. Brizhik, Davydov's soliton in an external alternating magnetic field. arXiv:2402.09172v1 [cond-mat.soft] 14 Feb 2024

[3] Karpman V. I., Maslov E. M. Perturbation theory for solitons. JETP 73 (1977) 537-559.

[4] L.S. Brizhik, J. Luo, B.M.A.G. Piette, W.J. Zakrzewski. Long-range electron

transport mediated by alpha-helices, Phys. Rev. E, 100 062205 (2019).

[5] L. Brizhik, E. Fermi, B. Zavan. Working principle of magnetic resonance therapy. J.Adv. Phys. 2015

**Acknowledgments:** This work was supported by the Department of Physics and Astronomy of the National Academy of Sciences of Ukraine (fundamental scientific program 0122U000887)

Special Session on Localized Excitations in Nonlinear Lattices (LENL) in <u>CHAOS2024</u>, Chania, Crete, Greece, June 11-14, 2024.

## Effects of self-correlated Gaussian noise on the emergence of robust breathers in the ac-driven, dissipative sine-Gordon model

Duilio De Santis<sup>1,\*</sup>, Giovanni Di Fresco<sup>1</sup>, Claudio Guarcello<sup>2</sup>, Bernardo Spagnolo<sup>1</sup>, Angelo Carollo<sup>1</sup>, Davide Valenti<sup>1</sup>

<sup>1</sup>Dipartimento di Fisica e Chimica "E. Segrè", Group of Interdisciplinary Theoretical Physics, Università degli Studi di Palermo, I-90128 Palermo, Italy <sup>2</sup>Dipartimento di Fisica "E. R. Caianiello", Università degli Studi di Salerno, I-84084 Fisciano, Salerno, Italy E-mail<sup>\*</sup>: duilio.desantis@unipa.it

**Abstract:** It has recently been established that thermal noise and harmonic forcing can cooperatively excite sine-Gordon breathers robust to dissipation. So far, this phenomenon has been therefore explored assuming a Gaussian noise source, delta-correlated both in time and space [1,2]. Given the potential implications of the present ideas, e.g., for the experimental observation of breathers in extended Josephson systems, it is particularly important to address the effects of more realistic noise sources with finite correlation time and/or correlation length. Here we show that breathers still emerge under this broader class of noise sources. Furthermore, we find that the correlation time and the correlation length offer control over the probability of observing breathers, a fact which can be very useful for the design of protocols aimed at detecting these elusive nonlinear excitations [3].

Keywords: Perturbed sine-Gordon model. Breathers. Self-correlated Gaussian noise.

#### References

[1] D. De Santis, C. Guarcello, B. Spagnolo, A. Carollo, D. Valenti, "Ac-locking of thermally-induced sine-Gordon breathers", Chaos, Solitons and Fractals 170 113382 (2023).

[2] D. De Santis, C. Guarcello, B. Spagnolo, A. Carollo, D. Valenti, "Noise-induced, ac-

# Thermalization slowing down for weakly nonintegrable many-body dynamics.

#### Sergej Flach

Institute for Basic Science, Daejeon, South Korea E-mail: sflach@ibs.re.kr

Abstract: We observe different universality classes in the slowing down of thermalization of many-body dynamical systems upon approaching integrable limits. We identify two fundamentally distinct long-range and short-range classes defined by the nonintegrable perturbation network spanned amongst the (set of countable) actions of the corresponding integrable limit. Weak two-body interactions (nonlinearities) induce long-range networks in translationally invariant lattices. Weak lattice coupling (hopping) instead induce short-range networks. For classical systems we study the scaling properties of the full Lyapunov spectrum. The long-range class results in a single parameter scaling of the Lyapunov spectrum, with the inverse largest Lyapunov exponent being the only diverging time control parameter and the rescaled spectrum approaching an analytical function. The short-range class results in a dramatic slowing down of thermalization and a rescaled Lyapunov spectrum approaching a non-analytic function. An additional diverging length scale controls the exponential suppression of all Lyapunov exponents relative to the largest one. For quantum spin chains we compute ergodization time scales within the framework of the Eigenstate Thermalization Hypothesis and the Lyapunov time from operator growth methods using Krylov Complexity. The comparison of both time scales confirms the existence of the above universality classes for quantum many body dynamics as well.

**Keywords:** Chaos, Thermalization, Nonintegrable Perturbations, Lyapunov Spectrum, Scaling, Universality, Eigenstate Thermalization Hypothethis, Krylov Complexity, Quantum Spin Chains

## Traveling Localized Vibrations in a Magnetically Coupled 2-DOF Resonators

#### Masayuki Kimura

Setsunan University, Neyagawa, Osaka, Japan E-mail: masayuki.kimura@setsunan.ac.jp

**Abstract:** A magnetically coupled 2-DOF resonators is fabricated to observe traveling localized vibrations and to study their characteristics experimentally. The 2-DOF resonator consists of an elastic rod and a permanent magnet. The magnet is attached to the top of the rod. Several rods are equally spaced and arranged in one dimension. The edge of the array is externally excited by a shaker. The amplitude and frequency of the shaker are carefully adjusted, and then traveling localized vibrations are successfully generated. We will discuss the condition of the amplitude and the frequency for generating the traveling localized vibrations.

Keywords: Intrinsic Localized Mode, Discrete Breather, Coupled Resonator Array, Nonlinear Vibrations and Waves in Lattices

Acknowledgments: This work is supported by JSPS Kakenhi No. 24K07393 and 21K03935.

## Development of nonmonotonically propagating annealing of defects with oscillating temperature at the wave front.

**Pavel Selyshchev** 

University of Pretoria, Pretoria, South Africa E-mail<sup>\*</sup>: selyshchev@gmail.com

**Abstract:** The most practical and fairly effective methods for recovering materials after irradiation is annealing of radiation defects namely disappearing of defects induced by heating, for example by means of recombination, etc. One of modes of annealing is a self-propagating annealing with constant speed and constant propagating profiles of temperature and defect density [1]. This annealing mode has the form of "stepped" distributions of temperature and defect density running at a constant speed. Before the wave front, the density of defects is constant and non-zero, and the temperature is equal to the ambient temperature. Behind the front, the density of defects is practically zero, and the temperature is increased. Annealing of defects occurs in the "annealing zone" - a narrow region of the "step" of the wave front.

Numerical investigation of this mode finds that for some set of parameters there are modes with oscillations of propagation speed and front of temperature profile. It has been found that oscillations of temperature takes place in the "annealing zone". In the annealed region, temperature disturbances have a form of temperature waves that follow temperature fluctuations in the "annealing zone." In the unannealed region, the temperature drops monotonically - temperature fluctuations do not have time to establish themselves due to the movement of the temperature front because an increase in temperature in the unannealed region leads to the annealing of defects in it and a displacement of the front of the wave. Temperature surges correspond to an increase in the steepness of the front of the defect annealing wave and an increase in the speed of its propagation.

It has been have established that these this mode develops due to thermo-concentration feedback, leading to instability of the mode with constant speed. The phenomenon was described using the theory of bifurcations. A criterion for the instability is obtained. An approximate analytical solution, which describes characteristic features for the post-bifurcation mode, is constructed.

Keywords: Defect annealing. Nonlinear feed-back. Self-propagating wave. Instability. Bifurcation.

#### References

[1] P. A. Selyshchev, P. M. Bokov. Kinetics of annealing: Basic relationships and nonlinear effects. In J. F. R. Archilla, F. Palmero, M. C. Lemos, B. Sánchez-Rey, and J. Casado-Pascual, editors, Nonlinear Systems, Vol. 2: Nonlinear Phenomena in Biology, Optics and Condensed Matter, pages 283–314. Springer International Publishing, Cham, 2018.